



# Art's Commerce and Science College, Onda

## Tal:- Vikramgad, Dist:- Palghar

My Inspiration  
Late. Shivlal  
Dhamone  
and  
Shri. V. G. Patil  
Saheb

Subject Teacher  
Santosh Dhamone

Practical No 3 : Condition of Compatibility of First Order Partial Differential Equations and  
Some Problem

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## Problem 1:

Show that the condition for  $f(x, y, z, p, q) = 0$  and  $g(x, y, z, p, q) = 0$  compatible is  $[f, g] = 0$   
i.e. 
$$\frac{\partial(f, g)}{\partial(x, p)} + \frac{\partial(f, g)}{\partial(y, q)} + p \frac{\partial(f, g)}{\partial(z, p)} + q \frac{\partial(f, g)}{\partial(z, q)} = 0$$

## Problem 2:

Show that the PDE  $xp = yq$  and  $z(xp + yq) = 2xy$  are compatible. Find Solution.



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### Problem 3:

Show that the PDE  $xp - yq = x$  and  $x^2p + q = xz$  are compatible. Hence find Solution